In this talk, we will explain a duality in Diophantine approximations, and as a consequence, we will develop a new approach to the perturbation theory for quasi-periodic motions, dealing only with periodic approximations and avoiding classical small divisors estimates. This is a joint work with Stphane Fischler (Orsay).